ALGEBRAIC FRACTIONS

To simplify algebraic fractions:

- 1. factorise the numerator and denominator
- 2. cancel any common factors

Example 11

Simplify:

(a)
$$\frac{9x+6}{3x+2}$$

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 (b) $\frac{15a^2-5ab}{10ab}$

(c)
$$\frac{9x^2 - y^2}{6xy - 2y^2}$$

Solution

(a)
$$\frac{9x+6}{3x+2} = \frac{3(3x+2)}{3x+2}$$

(b)
$$\frac{15a^2 - 5ab}{10ab} = \frac{5a(3a - b)}{10ab}$$
$$= \frac{3a - b}{2b}$$

bolution
(a)
$$\frac{9x+6}{3x+2} = \frac{3(3x+2)}{3x+2}$$
 (b) $\frac{15a^2 - 5ab}{10ab} = \frac{5a(3a-b)}{10ab}$ (c) $\frac{9x^2 - y^2}{6xy - 2y^2} = \frac{(3x-y)(3x+y)}{2y(3x-y)}$

$$= \frac{3a-b}{2b}$$

$$= \frac{3x+y}{2y}$$

Example 12
Simplify:
$$\frac{x^2 - 5x + 6}{x^2 - 9} \times \frac{x^2 + 3x}{x^2 - x - 2}$$

$$\frac{x^2 - 5x + 6}{x^2 - 9} \times \frac{x^2 + 3x}{x^2 - x - 2} = \frac{(x - 2)(x - 3)}{(x - 3)(x + 3)} \times \frac{x(x + 3)}{(x + 1)(x - 2)}$$
$$= \frac{x}{x + 1}$$