

## FACTORISING BY GROUPING IN PAIRS

Factorise:

$$1 \quad a(x+2) + b(x+2) \\ = (x+2)(a+b)$$

$$2 \quad 3a(2b-3c) - m(2b-3c) \\ = (2b-3c)[3a-m]$$

$$3 \quad p(a+b) + q(a+b) - r(a+b) \\ = (a+b)[p+q-r]$$

$$4 \quad x^2(2x-1) + 4(2x-1) \\ = (2x-1)(x^2+4)$$

$$5 \quad ax+4a+bx+4b \\ = a(x+4) + b(x+4) \\ = (x+4)(a+b)$$

$$6 \quad x^2 - xy + xz - yz \\ = x(x-y) + z(x-y) \\ = (x-y)(x+z)$$

$$10 \quad a^3 + 3a^2b + ab^2 + 3b^3 \\ = a^2(a+3b) + b^2(a+3b) \\ = (a+3b)(a^2+b^2)$$

$$11 \quad ac - 2bc - 2ad + 4bd \\ = c(a-2b) + d(-2a+4b) \\ = c(a-2b) - 2d(a-2b) \\ = (a-2b)(c-2d)$$

$$12 \quad 3xy - 6y + 7x - 14 \\ = y(3x-6) + 7(x-2) \\ = 3y(x-2) + 7(x-2) \\ = (x-2)(3y+7)$$

$$16 \quad x^3 + 3x^2 + 4x + 12 \\ = x^2(x+3) + 4(x+3) \\ = (x+3)(x^2+4)$$

$$17 \quad p^2q - pq^2 + 5p - 5q \\ = pq(p-q) + 5(p-q) \\ = (p-q)(pq+5)$$

$$18 \quad m^2p + m^2 + np + n \\ = m^2(p+1) + n(p+1) \\ = (p+1)(m^2+n)$$

$$19 \quad x^2y + x^2 + y + 1 \\ = x^2(y+1) + (y+1) \\ = (y+1)(x^2+1)$$

$$20 \quad ab - 3a - 4b + 12 \\ = a(b-3) - 4(b-3) \\ = (b-3)(a-4)$$

$$21 \quad 2x - 6y - xy + 3y^2 \\ = 2(x-3y) + y(-x+3y) \\ = 2(x-3y) - y(x-3y) \\ = (x-3y)(2-y)$$

22 When  $3m^2 - 3mn - m + n$  is factorised, the answer is:

- A  $(3m-1)(m-n)$      B  $(3m-n)(m-1)$      C  $(3m-1)(m+n)$      D  $(3m+1)(m-n)$

$$3m^2 - 3mn - m + n = 3m(m-n) - (m-n) = (m-n)(3m-1)$$

23 Indicate whether each answer is a correct or incorrect factorisation of  $2x^3 - 2x^2 - 2x + 2$ .

- (a)  $2(x+1)(x+1)(x-1)$      (b)  $2(x+1)(x-1)^2$      (c)  $2(x+1)(x-1)(x-1)$     (d)  $2(x-1)(x+1)^2$

$$2x^3 - 2x^2 - 2x + 2 = 2[x^3 - x^2 - x + 1] \\ = 2[x^2(x-1) - (x-1)] = 2[x-1][x^2-1] \\ = 2(x-1)(x-1)(x+1) \\ = 2(x-1)^2(x+1)$$