

SIMPLE HARMONIC MOTION (SHM)

- 1 The displacement x m of a particle moving in a straight line is given by $x = 6 \cos 4t$. Describe the motion of the particle.

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- 2 The equation of motion of a particle moving with simple harmonic motion is $\ddot{x} = -9x$. Find its period, amplitude and greatest speed if: (a) $x = 0, \dot{x} = 2$ when $t = 0$ (b) $x = 2, \dot{x} = 2$ when $t = 0$.

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- 3 A particle is moving in a straight line. If x metres is its displacement at time t seconds and $\left(\frac{dx}{dt}\right)^2 = 5(4 - x^2)$, find the acceleration in terms of x only. Show that the motion is simple harmonic and find its period and amplitude.

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- 8** A particle is moving along the x -axis in simple harmonic motion centred at the origin.
When $x = 2$, the velocity of the particle is 5.
When $x = 5$, the velocity of the particle is 4. Find:
- (a) the amplitude of the motion (b) the period of the motion.

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- 9 A particle moves in a straight line. At time t seconds, its displacement x cm from a fixed point O in the line is given by $x = 5 \cos\left(\frac{\pi}{2}t - \frac{\pi}{3}\right)$. Express the acceleration in terms of x only and hence show that the motion is simple harmonic. Find:
- (a) the period (b) the amplitude (c) the speed when $x = -2.5$ (d) the acceleration when $x = -2.5$.

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- 14 Solve the differential equation $\frac{d^2x}{dt^2} + 16x = 0$ subject to the conditions $x = 3$ and $\frac{dx}{dt} = 16$ when $t = 0$. Find the maximum displacement and the maximum speed if x metres is the displacement of the particle moving in a straight line at time t seconds.

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- 22** A floating buoy oscillates up and down with the waves, rising and falling 2 metres about its mean position. Find its greatest velocity and acceleration if the period of the motion is 3 seconds.

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- 29 A point moves with SHM in such a way that its speed is 8 and 6 m s^{-1} respectively at distances 3 and 4 m from the mean position. Calculate the period of the motion and the magnitude of the greatest acceleration.

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- 37** A particle is moving in a straight line under simple harmonic motion. It has a displacement of x metres from a point O , on the line, at time t seconds given by $x = 1 + 2 \cos\left(2t - \frac{\pi}{4}\right)$.
- (a) Show that $\ddot{x} = -4(x - 1)$.
 - (b) Find the centre of the motion and the time taken for the particle to first reach maximum speed.
 - (c) Find the amplitude of the motion and when the particle is first at rest.

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- 38** The tide can be modelled using simple harmonic motion. At a particular location, the depth at high tide is 5 metres and the depth at low tide is 1 metre. At this location, the tide completes two full periods every 25 hours. Let x represent the depth in metres and t be the time in hours after the first low tide of the day.
- (a) If this depth of this tide can be modelled by the function $x = a \cos nt + c$, find the values of a , n and c .
The first low tide today is at 2 a.m.
 - (b) At what time is the first high tide today?
 - (c) At what time this evening is the depth of water increasing at the fastest rate?