For questions 1 to 27, express each fraction with a rational denominator.

1
$$\frac{2}{\sqrt{3}}$$

2
$$\frac{\sqrt{5}}{\sqrt{3}}$$

3
$$\frac{3\sqrt{5}}{\sqrt{15}}$$

4
$$\frac{1}{\sqrt{3}-\sqrt{2}}$$

5
$$\frac{1}{2\sqrt{7}+\sqrt{6}}$$

6
$$\frac{1}{\sqrt{5}+2}$$

$$7 \frac{1}{2\sqrt{5}-3\sqrt{2}}$$

8
$$\frac{3\sqrt{2}}{\sqrt{5}-\sqrt{3}}$$

13
$$\frac{\sqrt{7} - 2\sqrt{5}}{3\sqrt{5} - 2\sqrt{2}}$$
 14 $\frac{3\sqrt{2} + 2\sqrt{3}}{3\sqrt{2} - 2\sqrt{3}}$ **15** $\frac{5\sqrt{3} + 3\sqrt{5}}{5\sqrt{5} - 3\sqrt{3}}$

14
$$\frac{3\sqrt{2} + 2\sqrt{3}}{3\sqrt{2} - 2\sqrt{3}}$$

15
$$\frac{5\sqrt{3}+3\sqrt{5}}{5\sqrt{5}-3\sqrt{3}}$$

16
$$\frac{2\sqrt{3}}{3\sqrt{3}-2}$$

21
$$\frac{\sqrt{3}}{\sqrt{24} - \sqrt{48}}$$
 22 $\frac{\sqrt{2} - 1}{\sqrt{2} + 1}$

22
$$\frac{\sqrt{2}-1}{\sqrt{2}+1}$$

23
$$\frac{2\sqrt{5}-\sqrt{2}}{2\sqrt{5}+\sqrt{2}}$$

23
$$\frac{2\sqrt{5}-\sqrt{2}}{2\sqrt{5}+\sqrt{2}}$$
 24 $\frac{\sqrt{6}+2\sqrt{3}}{2\sqrt{6}-\sqrt{3}}$

29 If
$$x = \sqrt{3} + 1$$
, find the value of $x^2 - \frac{1}{x^2}$.

For questions 36 to 44, express as a single fraction with a rational denominator:

$$36 \ \frac{1}{2\sqrt{3}-1} + \frac{3}{\sqrt{3}+1}$$

37
$$\frac{\sqrt{5} + \sqrt{2}}{\sqrt{5} - \sqrt{2}} - \frac{\sqrt{5} - \sqrt{2}}{\sqrt{5} + \sqrt{2}}$$

38
$$\frac{\sqrt{3}-\sqrt{2}}{\sqrt{3}+\sqrt{2}} \times \frac{2\sqrt{2}-\sqrt{3}}{2\sqrt{2}+\sqrt{3}}$$

42
$$\frac{\sqrt{3}-1}{\sqrt{3}+2} - \frac{\sqrt{5}-\sqrt{3}}{2\sqrt{5}+\sqrt{3}}$$

43
$$\frac{2\sqrt{5}}{\sqrt{10}-\sqrt{15}} - \frac{3\sqrt{7}}{\sqrt{35}-\sqrt{14}}$$

42
$$\frac{\sqrt{3}-1}{\sqrt{3}+2} - \frac{\sqrt{5}-\sqrt{3}}{2\sqrt{5}+\sqrt{3}}$$
 43 $\frac{2\sqrt{5}}{\sqrt{10}-\sqrt{15}} - \frac{3\sqrt{7}}{\sqrt{35}-\sqrt{14}}$ **44** $\frac{1}{x-1} + \frac{1}{x+1} - \frac{2}{x^2-1}$, where $x = 2\sqrt{3}+1$