1 Differentiate:

(a) 
$$e^{x^2} + 2$$

(b) 
$$(e^x + x^2)^4$$
  
(e)  $e^{\sqrt{x}+1}$ 

(c) 
$$e^x + ex$$

(d) 
$$4e^{\cos x}$$

(e) 
$$e^{\sqrt{x}+1}$$

(f) 
$$e^{x+\ln x}$$

- 2 Differentiate:
  - (a)  $x e^{\sin x}$
- **(b)**  $e^x \log_e x$
- (c)  $e^{\cos{(2x+1)}}$
- (d)  $1 + x + x^2 e^x$

**3** Given 
$$y = \frac{100}{1 + 15e^{-0.5t}}$$
, find  $\frac{dy}{dt}$ .

**5** In statistics, the normal probability density function is given by  $f(x) = \frac{1}{\sqrt{2\pi}}e^{-\frac{x^2}{2}}$ . Find f'(0).

- **4** (a) Sketch the graphs of  $f(x) = e^{\sin x}$  and  $g(x) = e^{\cos x}$  on the same diagram for  $0 \le x \le 2\pi$ , using appropriate technology.
  - **(b)** Write the coordinates of their points of intersection (correct to 3 decimal places where necessary). Check your solutions algebraically.
  - (c) Find the gradient of the tangent to each curve at their points of intersection.
  - (d) Do the curves intersect at right angles at these points? Justify your answer.