

THE SUBSTITUTION $t = \tan(A/2)$

2 Find: (a) $\int \frac{\sin x}{2 - \cos x} dx$ (b) $\int \frac{dx}{3 + 2 \cos x}$ (c) $\int \frac{dx}{1 + \sin x}$

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3 Evaluate: (a) $\int_0^{\frac{\pi}{3}} \sec x \, dx$ (b) $\int_0^{\frac{\pi}{2}} \frac{\sin \theta}{2 + \cos \theta} \, d\theta$

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4 Find: (a) $\int \frac{dx}{5 + 4 \cos x}$

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4 Find: (d) $\int \frac{dx}{3 - \cos x}$

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4 Find: (c) $\int \frac{\sin \theta}{2 + \sin \theta} d\theta$

Tip: Start by adding and subtracting 2 at the numerator.

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4 Find: (b) $\int \frac{\cos \theta}{2 - \cos \theta} d\theta$

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4 Find: (e) $\int \frac{\cos x}{\sin x + 1} dx$

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4 Find: (g) $\int \frac{\tan x}{1 + \cos x} dx$

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5 Using an appropriate substitution of the type $t = \tan x$, find: (a) $\int \frac{dx}{1 + \sin 2x}$

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5 Using an appropriate substitution of the type $t = \tan x$, find: (b) $\int \frac{\tan 2x}{1 + \cos 2x} dx$

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7 Use the substitution $t = \tan \frac{x}{2}$ to find $\int \frac{d\theta}{1 + \cos \theta + \sin \theta}$.

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9 Use the substitution $t = \tan \theta$ to find the exact value of $\int_0^{\frac{\pi}{4}} \frac{d\theta}{2 + \sin 2\theta}$.

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10 Using the substitution $t = \tan \frac{x}{2}$, or otherwise, evaluate $\int_{\frac{\pi}{3}}^{\frac{\pi}{2}} \frac{dx}{12 \sin x - 5 \cos x + 13}$.