# TRANSFORMATIONS OF GRAPHS OF TRIGONOMETRIC FUNCTIONS

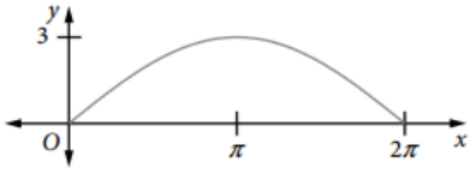
**1** Sketch the graph of each of the following, stating the period and amplitude of the function:

**(a)** $y = 4\sin x,\ 0 \le x \le 2\pi$ **(b)** $y = \cos 2x,\ 0 \le x \le 2\pi$ **(c)** $y = 3\tan x,\ -\frac{\pi}{2} \le x \le \frac{\pi}{2}$

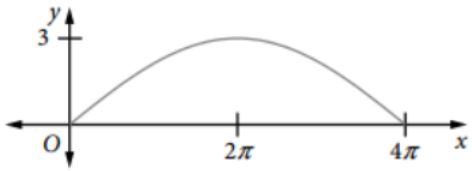
**(d)** $y = 4\sin 3x,\ 0 \le x \le 2\pi$ **(e)** $y = 3\cos 2x,\ 0 \le x \le 2\pi$ **(f)** $y = 3\tan 2x,\ -\frac{\pi}{2} \le x \le \frac{\pi}{2}$

**2** Which diagram shows the graph of $y = 3\sin\frac{x}{4}$ for $0 \le x \le 4\pi$?

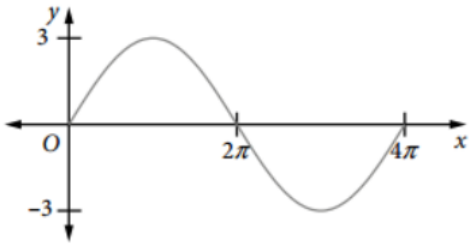
**A**



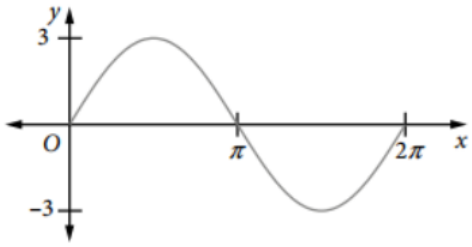

**B**




**C**




**D**



**3** Sketch the graph of each of the following, stating the period and amplitude of each function:

**(a)** $y = 3\sin\frac{x}{2}, -\pi \le x \le \pi$ **(b)** $y = 2\cos\frac{x}{2}, 0 \le x \le 2\pi$ **(c)** $y = 3\tan\frac{x}{2}, 0 \le x \le 2\pi$

**4** Sketch the graph of $y = \cos x, 0 \le x \le \pi$. On the same axes, sketch the graph of:

**(a)** $y = -\cos x$ **(b)** $y = 1 - \cos x$

**5** Sketch the graph of $y = \sin x, -\pi \le x \le \pi$. On the same axes, sketch the graph of:

**(a)** $y = 2\sin x$ **(b)** $y = -2\sin x$ **(c)** $y = 3 - 2\sin x$

**9** Sketch the graph of each of the following.

**(a)** $y = 2\sin\left(\theta - \frac{\pi}{2}\right)$ **(b)** $y = 3\cos\left(\theta + \frac{\pi}{4}\right)$ **(c)** $y = 2\sin(\theta - \pi)$

**(d)** $y = 5\cos 3\left(\theta + \frac{\pi}{3}\right)$ **(e)** $y = \frac{1}{2}\tan 2(\theta + \pi)$ **(f)** $y = \sqrt{2}\sin\left(2\theta - \frac{\pi}{2}\right)$

**10** Sketch the graph of each:

**(a)** $y = \sin 2\theta + 1$ **(b)** $y = 3\cos\theta - 2$ **(c)** $y = \frac{1}{2}\sin\left(\theta - \frac{\pi}{2}\right) + 3$

**(d)** $y = 2\cos 2\left(\theta - \frac{\pi}{4}\right) + 1$ **(e)** $y = 4\sin 3\left(\theta - \frac{\pi}{6}\right) - 2$ **(f)** $y = 3 - \sin\left(\theta - \frac{\pi}{2}\right)$

**11** By adding ordinates, sketch the graphs of:

**(a)** $y = \sin\theta + \cos\theta$ **(b)** $y = 3\sin 2\theta + 4\sin\theta$ **(c)** $y = 2\cos 3\theta + 3\sin 2\theta$

**(d)** $y = \sin 2\theta - \cos\theta$ **(e)** $y = \frac{1}{2}\cos 2\theta - \sin\theta$ **(f)** $y = \sin\theta + \sin 2\theta$

**13** By drawing appropriate graphs, solve each equation for $0 \le x \le 2\pi$.

**(a)** $\sqrt{3}\tan\left(x-\frac{\pi}{3}\right)-1=0$ **(b)** $2\sqrt{3}\cos\left(x+\frac{\pi}{4}\right)-3=0$ **(c)** $\sqrt{2}\sin\left(x+\frac{\pi}{6}\right)+1=0$