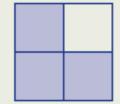
A fraction is made up of a numerator (up) and a denominator (down).

For example: $\frac{3}{5}$ — numerator denominator

- The **denominator** tells you how many parts the whole is divided up into.
- The **numerator** tells you how many of the divided parts you have selected.
- The horizontal line separating the numerator and the denominator is called the **vinculum**.
- We can represent fractions using area. If a shape is divided into regions of equal areas, then shading a certain number of these regions will create a fraction of the whole shape.

For example:



Fraction shaded = $\frac{3}{4}$

A **proper fraction** or **common fraction** is less than a whole, and therefore the numerator must be smaller than the denominator.

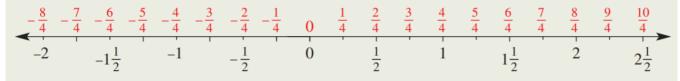
For example: $\frac{2}{7}$ is a proper fraction.

■ An **improper fraction** is greater than a whole, and therefore the numerator must be larger than the denominator.

For example: $\frac{5}{3}$ is an improper fraction.

■ We can represent positive and negative fractions on a number line.

This number line shows the whole numbers from -2 to 2. Each unit has then been divided equally into four segments, therefore creating 'quarters'.



■ Whole numbers can be represented as fractions.

On the number line above we see that 1 is the same as $\frac{4}{4}$ and 2 is the same as $\frac{8}{4}$.

Example 6 Understanding the numerator and the denominator

- a Into how many pieces has the whole pizza been divided?
- **b** How many pieces have been selected (i.e. shaded)?
- c In simplest form, when representing the shaded fraction of the pizza:
 - i what must the denominator equal?
 - ii what must the numerator equal?
 - iii write the amount of pizza selected (shaded) as a fraction.



SOLUTION

EXPLANATION

a 8

Pizza cut into 8 equal pieces.

b 3

3 of the 8 pieces are shaded in blue.

c i 8

Denominator shows the number of parts the whole has been divided into.

ii 3

Numerator tells how many of the divided parts you have selected.

... 3

Shaded fraction is the numerator over the denominator; i.e. 3 out of

8 divided pieces.

Example 7 Representing fractions on a number line

Represent the fractions $\frac{3}{5}$ and $\frac{9}{5}$ on a number line.

SOLUTION





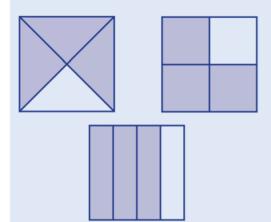
Draw a number line starting at 0 and mark on it the whole numbers 0, 1 and 2.

Divide each whole unit into five segments of equal length. Each of these segments has a length of one-fifth.

Example 8 Shading areas

Represent the fraction $\frac{3}{4}$ in three different ways, using a square divided into four equal regions.

SOLUTION



EXPLANATION

Ensure division of square creates four equal areas. Shade in three of the four regions.