

SOLVING TRIGONOMETRIC EQUATIONS

Give answers correct to 3 decimal places where necessary.

1 Solve each equation for $0^\circ \leq x \leq 180^\circ$.

(a) $3 + 2 \cos x = 5 \cos x$

(b) $\sin x = 3 \cos x$

(c) $6 \sin 2x = 3 \cos 30^\circ$

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Give answers correct to 3 decimal places where necessary.

1 Solve each equation for $0^\circ \leq x \leq 180^\circ$.

(d) $4 - 3 \tan x = \tan x$

(e) $3 \sin x = \cos x$

(f) $\sin 2x = \sin 30^\circ$

SOLVING TRIGONOMETRIC EQUATIONS

3 Solve each equation for $0^\circ \leq x \leq 360^\circ$.

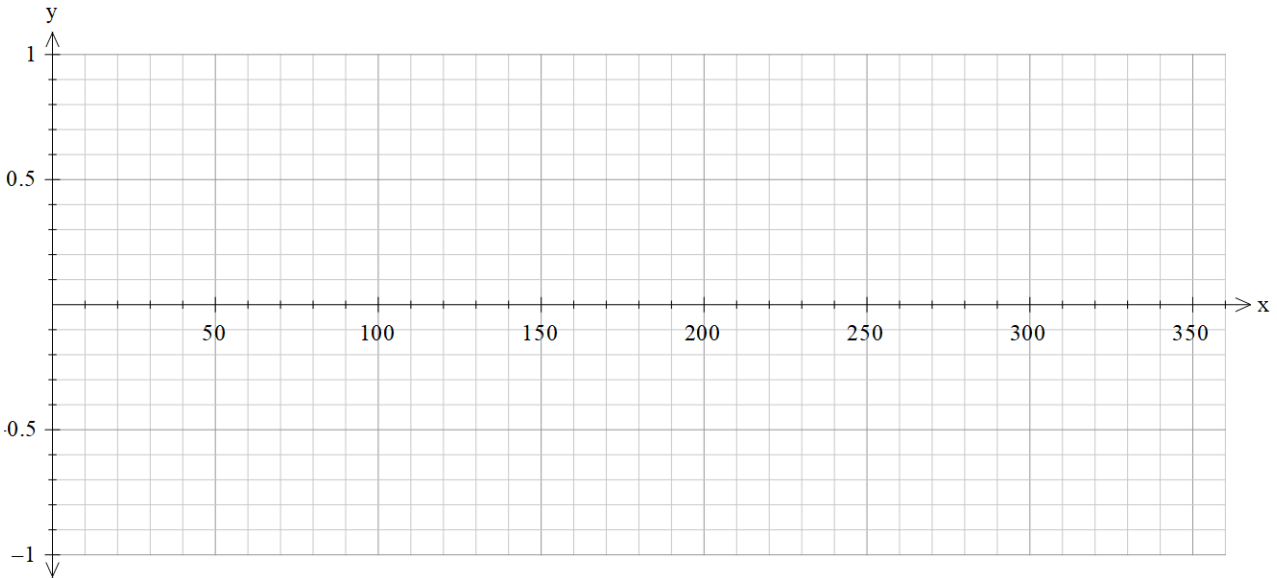
(a) $\operatorname{cosec}^2 x = 2$

(b) $\sin^2 x = 1$

(c) $\tan^2 x = 3$

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- 4 (a) On the same diagram draw $y = \sin x$ and $y = \frac{1}{2}$ for $0^\circ \leq x \leq 360^\circ$. Use your diagram to solve the equation $\sin x = \frac{1}{2}$ for $0^\circ \leq x \leq 360^\circ$.
- (b) What line would you need to draw to solve the equation $\sin x = -\frac{1}{2}$? What are the solutions to this equation for $0^\circ \leq x \leq 360^\circ$?



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5 Solve, for $0 \leq \theta \leq 2\pi$:

(a) $\sin \theta = \frac{-1}{\sqrt{2}}$

(b) $\sec \theta = \frac{2}{\sqrt{3}}$

(c) $\cot \theta = 1$

(d) $\sin^2 \theta - 2 \cos \theta + \cos^2 \theta = 0$

(e) $\sin^2 \theta + \cos \theta - 1 = 0$

(f) $\sec^2 \theta - 2 \tan \theta = 0$

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14 Solve for $0 < x < 2\pi$: **(a)** $5 \cos^2 x + 8 \sin x - 8 = 0$ **(b)** $6 \tan x = 5 \cot x$

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15 Simplify:

(a) $1 + \tan^2\left(\frac{\pi}{2} - \theta\right)$ (b) $1 - \cos^2(\pi + \theta)$ (c) $\sin \theta \cos\left(\frac{\pi}{2} - \theta\right) + \cos \theta \sin\left(\frac{\pi}{2} - \theta\right)$

(d) $\cos^2 \frac{\pi}{6} - 1$ (e) $1 - \sin \theta \cos\left(\frac{\pi}{2} - \theta\right)$

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18 Solve for $0 \leq \theta \leq 2\pi$:

(a) $3 \tan^3 \theta - 3 \tan^2 \theta - \tan \theta + 1 = 0$ (b) $\cos^3 \theta - 2 \cos^2 \theta + \cos \theta = 0$