

## THE INDEFINITE INTEGRAL

1 Find: (a)  $\int x \, dx$

(b)  $\int (x^2 + x + 1) \, dx$

(c)  $\int (3 - x^2) \, dx$

(d)  $\int (6x^5 - 4x^3 + 2x) \, dx$

(e)  $\int dx$

(f)  $\int x^n \, dx$

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2 Find: (a)  $\int \sqrt{x} \, dx$

(b)  $\int \frac{1}{x^2} \, dx$

(c)  $\int (1 + \sqrt{x} + x) \, dx$

3  $\int (1 + 2x + 3x^2) \, dx$  is equal to:

A  $x + x^2 + \frac{x^3}{3} + C$

B  $x + \frac{x^2}{2} + \frac{x^3}{3} + C$

C  $x + x^2 + x^3 + C$

D  $2 + 6x + C$

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4 If  $\frac{dy}{dx} = 1 + x + 3x^2$ , find the equation of the curve that passes through the point (2, 6).

5 If  $\frac{dy}{dx} = 1 + \sqrt{x}$ , find the equation of the curve that passes through the point (4, 10).

## PRIMITIVES OF TRIGONOMETRIC FUNCTIONS

1 Write the primitive function of:

(a)  $\sin 2x$

(b)  $\cos 3x$

(c)  $\sec^2 x$

(d)  $\sin x + \cos x$

(e)  $2 \sin x - 3 \cos x$

(f)  $\sin\left(x + \frac{\pi}{4}\right)$

(g)  $\cos \frac{x}{2}$

(h)  $2 \sin 2x$

2 The primitive of  $3 \cos \frac{x}{3}$  is:

A  $-\sin \frac{x}{3}$

B  $-9 \sin \frac{x}{3}$

C  $\sin \frac{x}{3}$

D  $9 \sin \frac{x}{3}$

## PRIMITIVES OF TRIGONOMETRIC FUNCTIONS

3 Find:

(a)  $\int \left( \sin \frac{\pi}{4} + \cos \frac{\pi}{4} \right) dx$

(b)  $\int (\sin x - \cos 2x) dx$

(c)  $\int \sin \left( 2x + \frac{\pi}{2} \right) dx$

(d)  $\int \cos \left( 2x - \frac{\pi}{4} \right) dx$

(e)  $\int \sec^2 3x dx$

(f)  $\int \left( \frac{1}{2} \sin 2x - \cos x \right) dx$

## PRIMITIVES OF TRIGONOMETRIC FUNCTIONS

- 4 (a) Differentiate  $f(x) = \log_e(\sin x)$       (b) Hence integrate  $\frac{\cos x}{\sin x}$

- 5 The gradient of a curve is given by  $\frac{dy}{dx} = 2 \sin 3x$ . If the curve passes through the point  $\left(\frac{\pi}{3}, 3\right)$ , find the equation of the curve.