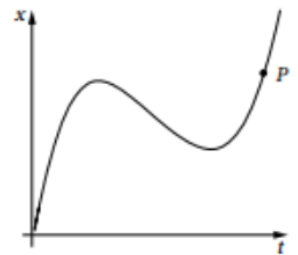


VELOCITY AND ACCELERATION AS RATES OF CHANGE

- 1 A particle is moving in a straight line, so that its displacement x metres from a fixed point O on the line at time t seconds ($t \geq 0$) is given by $x = 2t^3 - 5t^2 - 4t$.
- (a) Find the velocity and acceleration of the particle at any time t .
 - (b) Find the initial velocity and acceleration.
 - (c) When is the particle at rest?
 - (d) When is the acceleration zero? What is the velocity and displacement at this time?

- 4 The graph shows the displacement x of a particle moving along a straight line as a function of time t .
- Which statement best describes the motion of the particle at the point P ?
- A The velocity is negative and the acceleration is positive.
 - B The velocity is negative and the acceleration is negative.
 - C The velocity is positive and the acceleration is positive.
 - D The velocity is positive and the acceleration is negative.



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- 3 A particle moves in a straight line. Its velocity $v \text{ ms}^{-1}$ at time t is given by $v = 5 - \frac{10}{t+1}$.
- (a) Find the initial velocity.
 - (b) Find the acceleration of the particle when the particle is at rest.
 - (c) Sketch the graph of v for $t \geq 0$, showing any intercepts and asymptotes.

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5 The displacement of a particle moving along the x -axis is given by $x = 2t - \frac{1}{t+1}$, where x is the displacement from the origin in metres, t is in seconds and $t \geq 0$.

- (a) Find the expression for the velocity v and draw the graph of v against t .
- (b) What value does the velocity approach as t increases indefinitely?
- (c) Find the expression for the acceleration a and draw the graph of a against t .
- (d) Show that the acceleration of the particle is always negative.

6 A particle is moving along the x -axis. The displacement of the particle at time t is x metres. At a certain time, $v = -4 \text{ m s}^{-1}$ and $a = 3 \text{ m s}^{-2}$.

Which statement describes the motion of the particle at that time?

- A The particle is moving to the left with decreasing speed.
- B The particle is moving to the left with increasing speed.
- C The particle is moving to the right with decreasing speed.
- D The particle is moving to the right with increasing speed.

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- 7 A driver takes 3 hours to travel the distance between two points A and B on a country road. At time t hours after passing A , the driver's speed $v \text{ km h}^{-1}$ is given by $v = 60 + 40e^{-t}$.
- (a) Calculate the speeds when the driver passes points A and B .
 - (b) Write the acceleration in terms of: (i) t (ii) v
 - (c) Sketch the velocity-time curve and comment on the motion for large values of t .

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- 8 A particle moves in a straight line so that its displacement x from a fixed origin at any time t is given by $x(t) = 2(1 - e^{-t})$.
- (a) Find $x(0)$, $\dot{x}(0)$ and $\ddot{x}(0)$. (b) Sketch the graph of $x(t)$. (c) Find t when $x(t) = 1$.

- 9 A body starts from O and moves in a straight line. At any time t its velocity is given by $\dot{x} = 6t - 4$. Indicate whether each statement below is correct or incorrect.
- (a) $x = 3t^2 - 4t + C$ (b) $x = 3t^2 - 4t$ (c) $\ddot{x} = 3t^2 - 4t$ (d) $\ddot{x} = 6$

VELOCITY AND ACCELERATION AS RATES OF CHANGE

- 10** A body starts from O and moves in a straight line. At any time t , its velocity is $t^2 - 4t^3$. Find, in terms of t :
- (a) the displacement x (b) the acceleration.

- 11** The velocity $v \text{ m s}^{-1}$ at time t seconds ($t \geq 0$) of a body moving in a straight line is given by $v = 6t^2 + 6t - 12$. Find the acceleration at any time t .

VELOCITY AND ACCELERATION AS RATES OF CHANGE

- 12** A particle is projected vertically upwards from a point O with an velocity of 25 m s^{-1} and a downward acceleration of 10 m s^{-2} .
- (a) Find its velocity and height above O at any time t .
 - (b) What maximum height does the particle reach?
 - (c) At what time has its velocity been reduced to half the velocity of projection?

VELOCITY AND ACCELERATION AS RATES OF CHANGE

- 13** A body is projected vertically upwards with an initial velocity of 30 m s^{-1} . It rises with a deceleration of 10 m s^{-2} .
- (a) Find its velocity at any time t . (b) Find its height h m above the point of projection at any time t .
(c) Find the greatest height reached. (d) Find the time taken to return to the point of projection.