

# THEORETICAL PROBABILITY

If all outcomes in a sample space are equally likely, the **theoretical probability** of an event occurring is:

$$P(\text{event}) = \frac{\text{number of favourable outcomes}}{\text{total number of outcomes}}$$

A probability can be expressed as a fraction or decimal (ranging from 0 to 1) or a percentage (from 0% to 100%).

A event certain to occur has a probability of 1 (0 for an impossible event).

# EXAMPLE OF CALCULATION - PROBABILITY

This spinner has 5 equally divided sections.



**a** List the sample space using the given numbers.

**a**  $\{1, 2, 3, 3, 7\}$

**b** Find  $P(3)$ . **b**  $P(3) = \frac{2}{5}$  or 0.4

**c** Find  $P(\text{not a } 3)$ .

$$P(\text{not a } 3) = 1 - P(3) = 1 - \frac{2}{5} \text{ or } 1 - 0.4 = \frac{3}{5} \text{ or } 0.6$$

**d** Find  $P(\text{a } 3 \text{ or a } 7)$ .

$$P(\text{a } 3 \text{ or a } 7) = \frac{2}{5} + \frac{1}{5} = \frac{3}{5}$$

**e** Find  $P(\text{a number that is at least a } 3)$ .

$$\mathbf{e} \quad P(\text{at least a } 3) = \frac{3}{5}$$

# EXAMPLE OF CALCULATION - PROBABILITY

A letter is chosen from the word TELEVISION. Find the probability that the letter is:

**a** a V

**b** an E

**c** not an E

**d** either an E or a V

**a**  $P(V) = \frac{1}{10} (= 0.1)$

$$P(V) = \frac{\text{number of Vs}}{\text{total number of letters}}$$

**b**  $P(E) = \frac{2}{10}$   
 $= \frac{1}{5} (= 0.2)$

There are 2 Es in the word TELEVISION.

Simplify the fraction.

**c**  $P(\text{not an E}) = \frac{8}{10}$   
 $= \frac{4}{5} (= 0.8)$

If there are 2 Es in the word TELEVISION with 10 letters, then there must be 8 letters that are not E.

**d**  $P(\text{an E or a V}) = \frac{3}{10} (= 0.3)$

The number of letters that are either E or V is 3.