

## THE QUOTIENT RULE

1 Use the quotient rule to differentiate each function.

(a)  $y = \frac{x-1}{x+1}$

(b)  $f(x) = \frac{3x-7}{4x+5}$

(c)  $g(t) = \frac{2t+5}{t+2}$

## THE QUOTIENT RULE

1 Use the quotient rule to differentiate each function.

(g)  $y = \frac{4x^2}{2x+5}$

(h)  $y = \frac{4x^2 - 2}{x^2 + 5}$

(i)  $v(x) = \frac{x+1}{x^3-1}$

## THE QUOTIENT RULE

3 Differentiate each function with respect to  $x$ .

(a)  $y = \frac{\sqrt{x+1}}{x}$

(b)  $f(x) = \frac{(x+1)^2}{x}$

(c)  $y = \frac{x}{(x+1)^2}$

## THE QUOTIENT RULE

**3** Differentiate each function with respect to  $x$ .

(d)  $y = \frac{(2x+1)^3}{(3-x^2)^2}$

(e)  $f(x) = \frac{x}{\sqrt{x+1}}$

(f)  $y = \left(\frac{x+1}{x}\right)^2$

## THE QUOTIENT RULE

- 4  $f(x) = \frac{\sqrt{x}}{x^2+1}$ . Four steps in finding the simplest form of  $f'(x)$  are given. Indicate whether each step is correct or incorrect.

A  $f'(x) = \frac{(x^2+1) \times \frac{1}{2\sqrt{x}} - \sqrt{x} \times 2x}{(x^2+1)^2}$

B  $f'(x) = \frac{\frac{x^2+1}{2\sqrt{x}} - 2x\sqrt{x}}{(x^2+1)^2}$

C  $f'(x) = \frac{x^2+1-4x^2}{2\sqrt{x}(x^2+1)^2}$

D  $f'(x) = \frac{5x^2+1}{2\sqrt{x}(x^2+1)^2}$

- 5 Find the derivative of each function.

(a)  $y = (x^2 - 4)(x + 2)$

(b)  $f(x) = 4x^{\frac{5}{2}} - 2x^{\frac{3}{2}} + 6x^{\frac{1}{2}}$

(c)  $y = \sqrt{5x-1}$

## THE QUOTIENT RULE

5 Find the derivative of each function.

(k)  $y = (x^2 + 1)\sqrt{x}$

(l)  $g(x) = \frac{\sqrt{x+1}}{\sqrt{x^2+1}}$

6 Show that the gradient of the tangent to the curve  $y = \frac{x}{x^2+1}$  is zero twice, at  $x = -1$  and  $x = 1$ .