

THE SECOND DERIVATIVE AND CONCAVITY

1 Find $f''(x)$ for each function.

(a) $f(x) = 3x^2 + 5x + 6$

(b) $f(x) = x^3 + 2x^2 + 4x + 2$

(c) $f(x) = 24 - x^2$

3 Given $y = \frac{x^2 - 1}{x}$, find $\frac{d^2y}{dx^2}$. Indicate whether each statement below is a correct or incorrect step in finding $\frac{d^2y}{dx^2}$.

(a) $y = x - \frac{1}{x}$

(b) $\frac{dy}{dx} = \frac{x^2 - 1}{x^2}$

(c) $\frac{dy}{dx} = 1 + \frac{1}{x^2}$

(d) $\frac{d^2y}{dx^2} = \frac{-2}{x^2}$

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4 Find $\frac{d^2y}{dx^2}$ given: (a) $y = \sqrt{x}$ (b) $y = \sqrt{x-2}$ (c) $y = x\sqrt{x^2+1}$ (d) $y = \frac{1}{x}$

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4 Find $\frac{d^2y}{dx^2}$ given:

(f) $y = \frac{x}{x+3}$

(g) $y = \frac{x^2+1}{\sqrt{x}}$

(i) $y = \frac{\sqrt{x-1}}{x+1}$

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- 5 For what values of x is $y = 5x^2 - 1$ concave up?
- 6 For what values of x is $y = 6 - 3x^2$ concave down?
- 10 Explain why the graph of $y = \frac{1}{x^2}$ is concave up over its domain.