

RANDOM VARIABLES - CHAPTER REVIEW

- 1 For the uniform continuous variable with probability density function $f(x) = \begin{cases} k, & 0 \leq x \leq 10 \\ 0, & \text{otherwise} \end{cases}$, find the following values.
- (a) k (b) $P(X \leq 3)$ (c) $P(X \leq 5)$ (d) $P(2 \leq X \leq 9)$

- 2 Does the hybrid function $f(x) = \begin{cases} x^2 + 4x - \frac{10}{3}, & 0 \leq x \leq 3 \\ 0, & \text{otherwise} \end{cases}$ represent a probability density function?

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- 3 For the continuous variable with probability density function $f(x) = \begin{cases} \frac{x^2}{12}, & 0 \leq x \leq \sqrt[3]{36} \\ 0, & \text{otherwise} \end{cases}$, find the exact value of the median.

- 4 Honey is packed in jars with a labelled mass of 500 g. The actual amount X g of honey in the jar is such that $X \sim N(500, 25)$.
- (a) Find the probability that a jar chosen at random contains less than 495 g.
- (b) Jars containing less than 490 g cannot be sold. In a batch of 1000 how many jars would you expect to be rejected?

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5 If $X \sim N(12, 16)$, find the exact z values corresponding to the following x values.

- (a) $x = 8$ (b) $x = 20$

6 If $X \sim N(28, 16)$, find the exact z values corresponding to the following x values.

- (a) $x = 24$ (b) $x = 40$

7 If $f(x) = \begin{cases} \frac{2x}{15+k}, & 0 \leq x \leq 3 \\ 0, & \text{otherwise} \end{cases}$ defines a probability density function, then the value of k is:

- A $\frac{2}{15}$ B -6 C $-\frac{2}{15}$ D $\frac{1}{5}$

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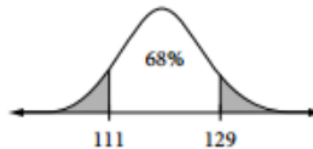
8 $X \sim N(10, 9)$. You would expect about 95% of observations to be in the range:

- A -8 to 28 B 0 to 28 C 10 to 19 D 4 to 16

9 Consider the following graph.

The graph is best described by:

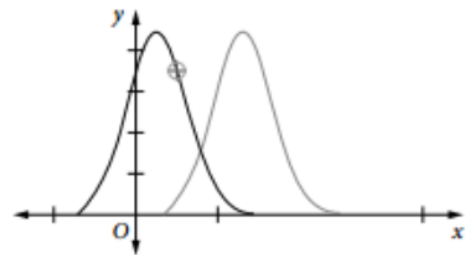
- A $N(111, 129)$ B $N(120, 81)$
 C $N(120, 3)$ D $N(120, 9)$



10 The graph shows two normal distributions drawn on the same set of axes. Graph 1 has a marker on it.

Compared to Graph 1, Graph 2 has:

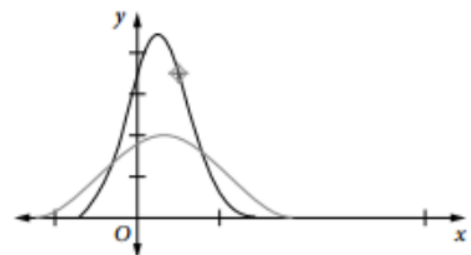
- A the same mean but a larger variation
 B the same mean but a smaller variation
 C the same variation but a larger mean
 D the same variation but a smaller mean



11 The graph shows two normal distributions drawn on the same set of axes. Graph 1 has a marker on it.

Compared to Graph 1, Graph 2 has:

- A the same mean but a larger variation
 B the same mean but a smaller variation
 C the same variation but a larger mean
 D the same variation but a smaller mean



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- 14** For their Mathematics assignment, Xandra and Zack have decided to record the times they spend completing the daily homework. Xandra's times are represented by the continuous random variable, X , in hours, with the probability density function:

$$f(x) = \begin{cases} -\frac{1}{9}(x^2 - 4x), & 0 \leq x \leq 3 \\ 0, & \text{otherwise} \end{cases}$$

Zack's times are represented by the continuous random variable, Z , in hours, with the probability density function:

$$f(z) = \begin{cases} \frac{2}{57}(z^2 - 9z + 20), & 0 \leq z \leq 3 \\ 0, & \text{otherwise} \end{cases}$$

- (a) Calculate the average time each student spends completing homework each day and compare the results. Xandra has a school concert to attend and has to complete her set homework within 1.5 hours.
- (b) Calculate the probability that Xandra will complete her homework in the required time.
- (c) Calculate the variance for the two variables.

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- 15** When fishing, fish shorter than a given length have to be thrown back into the water. Red snapper have a minimum allowed length of 30 cm and barramundi have a minimum allowed length of 55 cm. Let the variable R represent the lengths of red snapper caught, in cm, and the variable B represent the lengths of barramundi caught, in cm.

Observations of caught red snapper show that R is normally distributed with mean 36 and a variance of 9.

Observations of caught barramundi show that B is normally distributed with a variance of 16.

- (a) Calculate the mean length of barramundi caught, correct to the nearest whole number, if 2.5% of the barramundi caught are less than 54 cm.
- (b) Calculate the z -scores for the minimum allowed lengths for both variables, R and B , and interpret what this means in terms of which of the two species are more likely to be too small to keep.