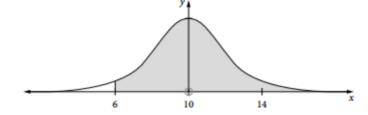
- 1 If  $X \sim N(15, 9)$ , find the exact z values corresponding to the following x values:
  - (a) 18
- **(b)** 21
- (c) 22
- (d) 16

- **2** Felipe has been applying for scholarships. On one particular test that followed the distribution  $X \sim N(40, 4)$ , he obtained a 42; and on another test that followed the distribution  $\sim N(75, 25)$ , he obtained an 82.
  - (a) Find the z value for the first test.
  - (b) Find the z value for the second test.
  - (c) On which test did Felipe do better?

- **3** A normal distribution graph is shown. If P(X > 14) = 0.35 then P(X > 6) is equal to:
  - A 0.35
- B 0.55
- C 0.65
- D 0.7

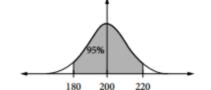


- 4 For a particular normal distribution you know that P(X < a) = 0.214 and P(X < b) = 0.496, where a < b. Find the following probabilities.
  - (a) P(X > a)
- **(b)** P(X > b) **(c)** P(a < X < b)

- **5** For  $Z \sim N(0, 1)$  it is known that P(Z < 0.85) = 0.8023. Find:

- (a) P(Z > 0.85) (b) P(Z < -0.85) (c) P(Z > -0.85) (d) P(-0.85 < Z < 0.85)

**7** Given the diagram below for *X* which follows a normal distribution, which of the following expressions best represents the shaded area? (*Z* represents the standard normal distribution.)



- A P(Z < 2)
- **B** P(-2 < Z < 2)
- **C** P(180 < Z < 220)
- **D** P(-0.2 < Z < 0.2)

- **8** X is a random variable that follows a normal distribution with a mean of 35 and a standard deviation of 7. The values of a and b are such that P(a < X < b) = 0.95 where this represents the middle 95% of values. a and b are best represented by:
  - **A** a = 23.49, b = 46.51
- **B** a = 21.28, b = 48.72
- C a = 29.11, b = 40.89
- **D** a = 21, b = 49

- 9 The distribution of weights for all 80.5 cm-tall girls in a population is such that the mean weight is 10.3 kg with a standard deviation of 0.8 kg.
  - (a) Adah is 80.5 cm tall and weighs 8.3 kg. What is Adah's z value for weight? These z values are used as a definition for some forms of malnutrition. Moderate acute protein-energy malnutrition is defined as having a z value in the range [-3.0, -2.0) and severe acute protein-energy malnutrition is defined as having a z value less than -3.0.
  - (b) Based on these definitions, what sort of acute protein-energy malnutrition would Adah be diagnosed with?
  - (c) Jamilah, who is also 80.5 cm tall, has been diagnosed with severe acute protein-energy malnutrition. What is Jamilah's weight, correct to one decimal place, less than?
  - (d) Another girl who is 80.5 cm tall, Xhosa, is not diagnosed with either form of acute protein-energy malnutrition. What is Xhosa's minimum weight?

- 10 The percentages obtained by a group of students in a Mathematics examination are represented by a random variable M and are normally distributed with a mean of 72 and a variance of 121. All percentages are rounded to the nearest whole percentage.
  - (a) Calculate the probability that a student obtained a mark of at least 50% (when rounded to the nearest whole percentage) in this examination, correct to four decimal places, and the number of standard deviations that this mark is below the mean.
  - **(b)** Determine the *z*-score of a student who obtained a mark of 45%. What is the expected mark of a student whose *z*-score has the same size but opposite sign from the student who scored 45%?

To obtain an A<sup>++</sup> mark, a student has to be in the top 2.5% of the group of students who have undertaken this examination.

(c) Calculate the minimum mark a student should obtain in this examination to be awarded an A<sup>++</sup> by first finding the corresponding z value.

The marks in the previous year's Mathematics examination were normally distributed with a mean of 70 and a variance of 144.

(d) Would a student who obtained a mark of 94% have been awarded an A<sup>++</sup> grade? Use appropriate calculations in your explanation.

- 11 Anita's daily charges for gas usage in her home form a normal distribution with an average daily cost of \$7.65 and a variance of 1.44, where the random variable C represents the daily cost for the gas used.
  - (a) What is the probability that in any one day Anita's cost is more than \$6.45?
  - (b) Determine the number of standard deviations from the mean for a cost of \$8.05 and a cost of \$6.65.
  - (c) Plot the two z values from part (b) on the normal distribution curve  $N(7.65, 1.2^2)$ .