

RATES OF CHANGE WITH RESPECT TO TIME

1 When concentrated chemical solutions are allowed to evaporate slowly, crystals are formed. The surface area of a particular crystal is given by $A = 0.8t^2$, where A is mm^2 and t is days of evaporation. The rate at which the surface area is increasing after 4 days is:

- A $0.8 \text{ mm}^2 \text{ day}^{-1}$ B $1.6 \text{ mm}^2 \text{ day}^{-1}$ C $6.4 \text{ mm}^2 \text{ day}^{-1}$ D $12.8 \text{ mm}^2 \text{ day}^{-1}$

2 The length of the sides of a square, x cm, is given by $x = 4t + 1$ where t is in seconds.

- (a) At what rate is the length of the side of the square increasing at t seconds?
- (b) At what rate is the length of the side of the square increasing when $t = 5$ seconds?
- (c) Write an expression for the area $A \text{ cm}^2$ of the square as a function of t .
- (d) At what rate is the area of the square increasing when $t = 5$ seconds?

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- 3** A petrol pump delivers petrol at the rate of 4 litres per minute.
- (a) How much petrol is delivered in 5 minutes?
 - (b) If V litres of petrol are delivered in t minutes at this rate, find an expression for V in terms of t .
 - (c) How much time will it take to deliver 45 litres of petrol?

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- 4 A tank holds 50 000 litres of water. The water drains from the tank in 40 minutes. The volume of water remaining in the tank after t minutes is given by $V = 50\,000\left(1 - \frac{t}{40}\right)^2$, where V is measured in litres.
- (a) Find the rate at which the water is draining from the tank after: (i) 5 minutes (ii) 10 minutes (iii) 20 minutes.
 - (b) How much water remains in the tank after 20 minutes?
 - (c) How much time will it take until only half the initial volume of water remains in the tank?

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- 5 The volume of water in a tank is given by $V = 1000 - 2t + \frac{t^2}{1000}$, where V is measured in litres and t is in minutes.
- (a) How much water is in the tank initially, assuming it was full?
 - (b) Find an expression for $\frac{dV}{dt}$ as a function of t .
 - (c) At what rate is the water flowing out of the tank at 25 minutes?
 - (d) How much time will it take to empty the tank at this rate?

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- 6 The rate at which solvent in a nail polish evaporates is given by $\frac{dV}{dt} = \frac{1}{500} \left(1 - \frac{t}{60} \right)$, where V mL is the volume of solvent present and t is in seconds.
- (a) What is the initial rate of evaporation of the solvent?
 - (b) When does the evaporation of the solvent stop?

